Epidemiologists study the distribution and determinants of disease frequency in human populations in order to control health problems. Thus, the objectives of epidemiology are to determine the extent of disease in a population, identify patterns and trends in disease occurrence, identify the causes of disease, and evaluate the effectiveness of prevention and treatment activities. Measuring how often a disease arises in a population is usually the first step in achieving these goals.

LEARNING OBJECTIVES
By the end of this chapter the reader will be able to:

■ Define and provide examples of a population.
■ Distinguish between a fixed and dynamic (or open) population.
■ Explain how epidemiologists create a case definition and discuss how the definition of acquired immunodeficiency syndrome (AIDS) has changed over time.
■ Describe the key aspects of measuring disease occurrence.
■ Define and distinguish between cumulative incidence, incidence rate, and prevalence.
■ Describe the mathematical relationship between the measures of disease frequency.
■ Provide examples of commonly used measures of disease frequency in public health.

Introduction
Epidemiologists study the distribution and determinants of disease frequency in human populations in order to control health problems. Thus, the objectives of epidemiology are to determine the extent of disease in a population, identify patterns and trends in disease occurrence, identify the causes of disease, and evaluate the effectiveness of prevention and treatment activities. Measuring how often a disease arises in a population is usually the first step in achieving these goals.
This chapter describes how epidemiologists quantify the occurrence of disease in a population. Readers will learn that this quantification process involves developing a definition of a particular disease, counting the number of people who are affected by the disease, determining the size of the population from which the diseased cases arose, and accounting for the passage of time.

**Definition of a Population**

Because epidemiology is concerned with the occurrence of disease in groups of people rather than in individuals, populations are at the heart of epidemiologists’ measurements. A population can be defined as a group of people with a common characteristic such as place of residence, religion, gender, age, use of hospital services, or life event (such as giving birth).

Location of residence such as a country, state, city, or neighborhood is one of the most common ways to define a population. For example, the people who reside in the Brooklyn borough of New York City, the city of Boston, the state of Oregon, and the country of Sweden are members of distinct populations defined by geopolitical entities ranging in size from a neighborhood to an entire country. Residence near natural geographic features such as rivers, mountains, lakes, or islands can also be used to define a population. For example, people who live along the 2,350-mile length of the Mississippi River, around Mount St. Helens in Washington State, and on Nantucket Island off the coast of Massachusetts are members of populations defined by geographic formations.

Because epidemiology focuses on disease occurrence, populations are commonly defined in relation to a medical facility such as a doctor’s office, clinic, or hospital. The service population of a medical facility (also called *catchment population*) consists of the people who use the facility’s services. This population is often difficult to define because an individual’s decision to use a facility may depend on how far it is from home, the person’s particular medical condition, his or her type of medical insurance, and so forth.

Consider a situation in which a county has only one general hospital, which provides the complete range of medical services including preventive care, birthing services, and diagnostic and therapeutic services for acute and chronic conditions. The catchment population for this general hospital is likely to consist of all people who live in the county where the hospital is located (see Figure 2–1).

Now suppose that this hospital enhances its cardiology department, adding many well-trained clinicians and the latest diagnostic equipment. As the cardiology department’s reputation for excellent care grows, patients travel from greater distances to receive care. As a result, the catchment population for the cardiology department expands to the
surrounding counties while the catchment population for the other hospital services, particularly those dealing with acute conditions requiring prompt treatment, remains the single county where the hospital is situated (see Figure 2–1).

Socioeconomic status is still another determinant of hospital catchment populations. Consider a city in which there are two hospitals—one public and one private—located within a few miles of each other. The private hospital generally treats patients with medical insurance, and the public hospital mainly treats patients without insurance. Even though each catchment population resides roughly within the same geographic area, the two
service groups are distinct in terms of income, and probably many other factors (see Figure 2–1).

Still another way that a population can be defined is by the occurrence of a life event such as undergoing a medical procedure, giving birth to a child, entering or graduating from school, or serving in the military. For example, students who graduated from college in 2011 are members of the population known as the “Class of ’11,” and the men and women who served in the U.S. military during the War in Iraq are members of the population known as Iraq War veterans. Populations are often defined by other characteristics such as age, gender, religion, or type of job.

A unifying framework for thinking about a population is whether its membership is permanent or transient (see Table 2–1). A population whose membership is permanent is called a fixed population. Its membership is always defined by a life event. For example, the people who were in Hiroshima, Japan, when the atomic bomb exploded at the end of World War II are members of a fixed population. This population will never gain any new members because only people who were at this historical event can be members.

The opposite of a fixed population is a dynamic or open population. Its membership is defined by a changeable state or condition and so is transient. A person is a member of a dynamic population only as long as he or she has the defining state or condition. For example, the population of the city of Boston is dynamic because people are members only while they reside within the city limits. Turnover is always occurring because people enter the city by moving in or by birth, and people leave the city by moving away or by death. The term steady state describes a situation in which the number of people entering the population is equal to the number leaving. Dynamic populations include groups defined by geographic and hospital catchment areas, religious groups, and occupations.

Regardless of the way in which it is defined, a population can be divided into subgroups on the basis of any characteristic. For example, men who undergo coronary bypass surgery are a gender subgroup of a fixed population defined by a life event, and all children up to 6 years of age who live along the Mississippi River are an age subgroup of a dynamic population defined by a geographic formation.

<table>
<thead>
<tr>
<th>Type of population</th>
<th>Key element</th>
<th>Example</th>
</tr>
</thead>
<tbody>
<tr>
<td>Fixed</td>
<td>Membership is based on an event and is permanent</td>
<td>Japanese atomic bomb survivors</td>
</tr>
<tr>
<td>Dynamic or open</td>
<td>Membership is based on a condition and is transitory</td>
<td>Residents of a city, hospital patients</td>
</tr>
</tbody>
</table>
Definitions of Health and Disease

In 1948, the World Health Organization defined health as “a state of complete physical, mental and social well-being and not merely the absence of disease or infirmity.” More recently, a national plan for improving the health of the American people, stated that health is a key aspect of the quality of life and that it “reflects a personal sense of physical and mental health and the ability to react to factors in the physical and social environments.” The plan also states that the “health-related quality of life is more subjective than life expectancy and therefore can be more difficult to measure.”

Because measurement is a cornerstone of epidemiology, and “health” and “a sense of well-being” are nonspecific and difficult to quantify, epidemiologists have almost entirely focused their activities on the “absence of health,” such as specific diseases, injuries, disabilities, and death. Consequently, epidemiologists must first compose a definition of the “absence of health” or “disease” before they can begin measuring its frequency.

The definition of a disease is usually based on a combination of physical and pathological examinations, diagnostic test results, and signs and symptoms. Which and how many criteria are used to define a “case” (a person who meets the disease definition) has important implications for accurately determining who has the disease.

Consider the various criteria that can be used to define a heart attack case. One could use the symptoms of chest pain, the results of diagnostic tests such as electrocardiograms, or blood enzyme tests for cardiac damage. What are the implications of using only chest pain to define heart attack cases? Using only this nonspecific symptom will capture most but not all people who have heart attacks because it will miss people who have “silent” heart attacks, which occur without chest pain. In addition, it will erroneously include many people who have other conditions that produce chest pain, such as indigestion.

A definition that includes more specific criteria such as the results of diagnostic tests will be more accurate. For example, if positive blood enzyme tests are included, silent heart attacks are likely to be picked up and the other conditions that cause chest pain omitted. In practice, epidemiologists use all available information from physical and pathological examinations, and laboratory and other tests to define a case of a disease as accurately as possible.

Changes in Disease Definitions

Even when clear-cut criteria are used, disease definitions often change over time as more is learned about a disease and its various manifestations. For example, the official definition of acquired immune deficiency
syndrome (AIDS) has been changed several times as researchers have gained knowledge about the disease’s cause and natural course (see Table 2–2).

The story began in the summer of 1981 when the Centers for Disease Control and Prevention (CDC) reported that Kaposi’s sarcoma and Pneumocystis carinii pneumonia had been observed among previously healthy homosexual men.5 Previously, Kaposi’s sarcoma, a malignant neoplasm of the blood vessels, had been seen primarily among elderly males, and opportunistic infections such as Pneumocystis carinii pneumonia had occurred almost exclusively in people with compromised immune systems.

In 1982, the CDC composed the first definition of AIDS for national reporting as “a disease, at least moderately predictive of a defect in cell-mediated immunity, occurring in a person with no known cause for diminished resistance to that disease . . . including Kaposi’s sarcoma, Pneumocystis carinii pneumonia, and serious other opportunistic infections.”6 Even then, the CDC acknowledged that the case definition was imperfect because it could
possibly miss the full range of AIDS manifestations and falsely include individuals who were not truly immunodeficient. However, because the cause of AIDS was unknown at that time, the definition at least served as a consistent tool for monitoring the epidemic.

The CDC made the first major change in the official AIDS case definition in 1985 after the human immunodeficiency virus (HIV) was determined to be the cause of AIDS, and a highly accurate laboratory test was developed to detect the antibody to the HIV virus. Because epidemiologists now knew what to look for and how to find its trail, it was possible to expand the AIDS case definition from a few severe clinical conditions to a wide range of conditions accompanied by laboratory evidence of HIV infection. Conversely, it also became possible to exclude patients who had AIDS-like symptoms but had negative HIV antibody test results.

At the end of 1992, the CDC changed the AIDS case definition again after natural history studies revealed the importance of lymphocytes in the HIV infection. The new definition was expanded to include individuals who had no symptoms of AIDS but had low levels of CD4 T lymphocytes, a type of white blood cell that is responsible for fighting off infections. (These cells are the primary target of HIV and are an excellent marker of disease progression.) In 2008, the CDC further refined the disease definition by combining HIV infection and AIDS into a single case definition and requiring laboratory confirmation of infection.

In summary, as epidemiologists discovered the cause of AIDS, learned more about its different manifestations, and developed a test to detect HIV, the AIDS case definition was expanded from a few severe diseases to many varied conditions and the results of sophisticated laboratory tests (see Table 2–2).

What impact did these changes in case definition have on the number of reported AIDS cases? In general, any expansion in the case definition will increase the number of reportable cases, and any contraction will decrease that number. With AIDS, the definition changes increased the number of people who were officially counted as AIDS cases in national statistics from the 1980s until 1993. However, AIDS incidence subsequently declined due to the introduction of highly active antiretroviral therapy despite the 1993 expanded case definition.

**Measuring Disease Occurrence**

Epidemiologists must always consider three factors when they measure how commonly a disease occurs in a group of people: (1) the number of people that are affected by the disease, (2) the size of the population from which the cases of disease arise, and (3) the length of time that the population is followed. Failure to consider all three components will give a false impression about the impact of the disease on a population.
Consider the following hypothetical data on the frequency of breast cancer in two counties. In County A, with a population of 50,000, a total of 100 new cases of breast cancer occurred over a 1-year period. In County B, with a population of 5,000, 75 new cases occurred over a 3-year period. Which county has a higher frequency of new breast cancer cases? If one considers only the number of new cases, it appears that County A has a higher frequency (100 versus 75). However, simply comparing the number of cases in each town does not provide a full picture because the cases occurred over different lengths of time (1 versus 3 years) and among populations of different sizes (50,000 versus 5,000) (see Table 2–3).

In order to make a meaningful comparison between the two counties, it is necessary to convert the data into the same population size and time period. Let us estimate the frequency of breast cancer in the two counties over a 1-year period and as if each population consisted of 100,000 people. The frequency of breast cancer in County A is 100 cases/50,000 population/1 year; if the county’s population were 100,000, the frequency would double to become 200 cases/100,000 population/1 year.

Two steps are needed to make a similar conversion for County B: (1) divide the numerator by 3 to convert the frequency of breast cancer from a 3- to a 1-year period: 25 cases/5,000 population/1 year; (2) multiply both the numerator and denominator by 20 to estimate the frequency for a population of 100,000. Thus, the frequency of new cases in County B is 500 cases/100,000 population/1 year.

Now it is clear that the “rate” at which new cases are occurring is much higher in County B than County A (500 cases/100,000 population/1 year versus 200 cases/100,000 population/1 year, respectively), and that examining only the number of new cases gives a false impression. Note that the decision to convert the frequencies to a population size of 100,000 and a 1-year time period, while commonly done, is arbitrary. Other population sizes (such as 1,000 or 10,000) and time periods (such as 1 month or 5 years) could be used. The guiding principle is that the same population size and time period should be used for the compared groups.

<table>
<thead>
<tr>
<th>Type of data</th>
<th>County A</th>
<th>County B</th>
</tr>
</thead>
<tbody>
<tr>
<td>Number of cases</td>
<td>100</td>
<td>75</td>
</tr>
<tr>
<td>Population size</td>
<td>50,000</td>
<td>5,000</td>
</tr>
<tr>
<td>Follow-up period</td>
<td>1 year</td>
<td>3 years</td>
</tr>
<tr>
<td>Comparable disease frequency</td>
<td>200/100,000/year</td>
<td>500/100,000/year</td>
</tr>
</tbody>
</table>
Types of Calculations: Ratios, Proportions, and Rates

Three types of calculations are used to describe and compare measures of disease occurrence: ratios, proportions, and rates (see Table 2–4). A ratio is simply one number divided by another. The entities represented by the two numbers are not required to be related to one another. In other words, the individuals in the numerator can be different from those in the denominator. For example, the “gender ratio” is a ratio of two unrelated numbers: the number of males divided by the number of females, usually expressed as the number of males per 100 females. In recent U.S. Census data, the gender ratio among U.S. residents aged 80–84 years was 66.5 males per 100 females.11

A proportion is also one number divided by another, but the entities represented by these numbers are related to one another. In fact, the numerator of a proportion is always a subset of the denominator. Proportions, also known as fractions, are often expressed as percentages and range from 0 to 1 or 0% to 100%. For example, the proportion of U.S. residents who are Black is the number of Black residents divided by the total number of U.S. residents of all races. In recent U.S. Census data, the proportion of Black U.S. residents was 0.123 or 12.3%.12 The remaining proportion included Whites (0.724 or 72.4%) and other or multiple races (0.153 or 15.3%). Note that these three proportions add up to 100% because the three groups (Black, White, and all other races) are collectively exhaustive.

A rate is also one number divided by another, but time is an integral part of the denominator. We are familiar with rates in our daily travels since a rate is a measure of how fast we travel. For example, in many areas of the United States, the maximum speed or rate at which cars are permitted to travel is 55 miles per hour. This rate can also be written as 55 miles/1 hour. The measure of time in the denominator is what makes this number a rate. The measures of disease occurrence calculated previously for Counties A and B are also rates (200 cases/100,000 population/1 year and 500 cases/100,000 population/1 year, respectively). Unfortunately, the term rate is often incorrectly used to describe ratios and proportions.13

<table>
<thead>
<tr>
<th>Type of Calculation</th>
<th>Characteristics</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ratio</td>
<td>Division of two unrelated numbers</td>
</tr>
<tr>
<td>Proportion</td>
<td>Division of two related numbers; numerator is a subset of denominator</td>
</tr>
<tr>
<td>Rate</td>
<td>Division of two numbers; time is always in denominator</td>
</tr>
</tbody>
</table>
Measures of Disease Frequency

The two basic measures of disease frequency in epidemiology are incidence and prevalence. *Incidence* measures the occurrence of new disease, and *prevalence* measures the existence of current disease. Each measure describes an important part of the natural course of a disease. Incidence deals with the transition from health to disease, and prevalence focuses on the period of time that a person lives with a disease.

**Incidence**

Incidence is defined as the occurrence of new cases of disease that develop in a candidate population over a specified time period. There are three key ideas in this definition.

First, incidence measures *new disease events*. For diseases that can occur more than once, it usually measures the first occurrence of the disease. Second, new cases of disease are measured in a *candidate population*, which is a population of people who are “at risk” of getting the disease. Someone is at risk because he or she has the appropriate body organ, is not immune, and so forth. For example, a woman who still has an intact uterus (i.e., she has not undergone a hysterectomy) is a candidate for getting uterine cancer, and a child who has not been fully immunized against the polio virus is a candidate for contracting poliomyelitis. Although it is possible to define and measure the incidence of disease in a population not at risk (e.g., the incidence of uterine cancer in women who have undergone hysterectomies is, by definition, zero), it is not a particularly interesting pursuit.

Third, incidence takes into account the *specific amount of time* that the members of the population are followed until they develop the disease. Because incidence measures a person’s transition from a healthy to a diseased state, time must pass for this change to occur and be observed. As described in the following sections, there are two types of incidence measures: cumulative incidence and incidence rate. Although closely related, each measure has different strengths and weaknesses and is used in different settings.

**Cumulative Incidence**

Cumulative incidence is defined as the proportion of a candidate population that becomes diseased over a specified period of time. Mathematically, it is expressed as follows:

\[
\frac{\text{Number of new cases of disease}}{\text{Number in candidate population}} \text{ Over a specified time period}
\]
Note that the numerator (new cases of disease) is a subset of the denominator (candidate population), and so the possible value of cumulative incidence ranges from 0 to 1 or, if expressed as a percentage, from 0% to 100%. Time is not an integral part of this proportion but rather is expressed by the words that accompany the numbers of the cumulative incidence measure. Thus, cumulative incidence is dimensionless (see Table 2–5).

Cumulative incidence can be thought of as the average risk of getting a disease over a certain period of time. (A risk is the probability of getting a disease.) A commonly cited measure of cumulative incidence is the “lifetime risk of breast cancer” among women. Currently estimated at “one in eight” among U.S. women, it means that 13% of women will develop breast cancer sometime during the course of their lives. Cumulative incidence is influenced by the length of time to which it applies. Generally, the cumulative incidence over a long period of time (such as a lifetime) will be higher than that over a few years.

Cumulative incidence is mainly used in fixed populations when there are no or small losses to follow-up. Consider, for example, the estimated 255,000 residents of Hiroshima, Japan, who were present in the city when the atomic bomb was dropped on August 6, 1945 (see Figure 2–2). During the blast and in the weeks and months immediately thereafter, an estimated 65,000 people died from physical trauma, burns, and acute radiation sickness, resulting in a 25% cumulative incidence of mortality over a 4-month period. Officials estimate that another 21% of the population died during the year following that initial 4-month period. During the subsequent years and decades, the cumulative incidence of death was much lower, and different causes of death such as cancer predominated.

### Table 2–5: Distinguishing Characteristics of Incidence and Prevalence

<table>
<thead>
<tr>
<th>Measure</th>
<th>Type of number</th>
<th>Units</th>
<th>Range</th>
<th>Numerator</th>
<th>Denominator</th>
<th>Major uses</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cumulative incidence</td>
<td>Proportion</td>
<td>None</td>
<td>0 to 1</td>
<td>New cases</td>
<td>Population at risk</td>
<td>Research on causes, prevention, and treatment of disease</td>
</tr>
<tr>
<td>Incidence rate</td>
<td>True rate</td>
<td>1/time or $t^{-1}$</td>
<td>0 to infinity</td>
<td>New cases</td>
<td>Person-time at risk</td>
<td>Research on causes, prevention, and treatment of disease</td>
</tr>
<tr>
<td>Prevalence</td>
<td>Proportion</td>
<td>None</td>
<td>0 to 1</td>
<td>Existing cases</td>
<td>Total population</td>
<td>Resource planning</td>
</tr>
</tbody>
</table>

Note that the numerator (new cases of disease) is a subset of the denominator (candidate population), and so the possible value of cumulative incidence ranges from 0 to 1 or, if expressed as a percentage, from 0% to 100%. Time is not an integral part of this proportion but rather is expressed by the words that accompany the numbers of the cumulative incidence measure. Thus, cumulative incidence is dimensionless (see Table 2–5).
cumulative incidence of death was about 60% over the 50-year period from 1950 through 2000 among Hiroshima and Nagasaki survivors who were enrolled in the Life Span Cohort Study of the effects of high-dose radiation on the incidence of disease and death.\textsuperscript{16}

Note that the cumulative incidence of death during the first 16 months after the bomb was dropped (25% + 21% = 46%) was close to that during the 50-year follow-up period of the Life Span Cohort Study (60%). This finding underscores the importance of describing the time period that the measure covers.

Everyone in the Hiroshima atomic bomb population will eventually die, and the cumulative incidence of mortality will ultimately be 100%. In addition, the size of the candidate population dwindles as members die. For example, all 255,000 residents were at risk of dying when the bomb was dropped in August 1945, while approximately 190,000 survivors of the initial period were at risk of dying during the subsequent years (see Figure 2–2).

One critical assumption underlies the cumulative incidence measure. Everyone in the candidate population has been followed for the specified time period. Thus, the estimate that women have a 13% lifetime risk of breast cancer assumes that a population was followed for incidence of breast cancer from birth until death, an average of 70 to 80 years. Complete follow-up is difficult to attain, particularly in a dynamic population in

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{figure2-2.png}
\caption{Dwindling Size of the Hiroshima Atomic Bomb Population over Time: 1945–2000}
\end{figure}
which members are continually entering and exiting. Thus, cumulative incidence is usually reserved for fixed populations, particularly when there are no or few losses to follow-up.

**Incidence Rate**

Incidence rate is defined as the occurrence of new cases of disease that arise during person-time of observation. Mathematically, the incidence rate is expressed as follows:

\[
\frac{\text{Number of new cases of disease}}{\text{Person-time of observation in candidate population}}
\]

Note that the numerator for incidence rate is identical to that of cumulative incidence. The difference between the two measures lies in the denominator. The incidence rate’s denominator integrates time (t), and so it is a true rate.\(^\text{13}\) Thus, its dimension is 1/t or t\(^{-1}\), and its possible values range from zero to infinity (Table 2–5). An incidence rate of infinity is possible if all members of a population die instantaneously.

The concept of person-time can be difficult to understand. Person-time is accrued only among candidates for the disease. Thus, a person contributes time to the denominator of an incidence rate only up until he or she is diagnosed with the disease of interest. However, unlike for cumulative incidence, the incidence rate is not based upon the assumption that everyone in the candidate population has been followed for a specified time period. Person-time is accrued only while the candidate is being followed. Accrual of person-time stops when the person dies or is lost to follow-up (such as when a person moves away from a community). The incidence rate can be calculated for either a fixed or dynamic population. However, because it directly takes into account population changes (such as migration, birth, and death), it is especially useful as a measure of the transition between health and disease in dynamic populations.

Consider the following population of a hypothetical town (Figure 2–3). This dynamic population of five individuals is followed for the 10-year period from 2000 to 2010. Person A moved into town in 2001, was diagnosed with disease in 2005, and so accrued 4 years of person-time. Person B was a resident of the town at the start of the observation period in 2000, died in 2006, and so accrued 6 person-years. Person C moved to town in 2002 and remained healthy until he moved away in 2005. The investigator could not determine where he moved and so could not learn if he became diseased later. Person C was considered lost to follow-up as of the time he moved, and so he accrued 3 person-years. Person D was a resident of the town at the start of the observation period, remained healthy for the entire period, and so accrued 10 years of person-time. Person E was born to
Person A in 2003, remained healthy for the entire observation period, and so accrued 7 person-years.

The incidence rate in this hypothetical population is 1/30 person-years. Only one person became diseased and 30 person-years of observation were accrued by the population. The denominator of the incidence rate is the sum of person-time accrued by each member of the population at risk.

Now consider an actual population of 106,841 Scandinavian women who were studied to quantify the effect of physical activity on overall mortality. The women were enrolled during 1991–1992 and followed through 2003 to determine their vital status. Each woman’s follow-up time began with the date of return of her questionnaire during 1991–1992 and continued until one of the following events occurred: death, emigration, or end of follow-up for the study. There were virtually no losses to follow-up because of Scandinavia’s excellent population registers that are continuously updated for mortality. Investigators identified 141 deaths among the 52,665 person-years of follow-up among women who were not physically active in contrast to 75 deaths among 86,016 person-years of follow-up among women who had very high levels of activity. Although it is most accurate to determine person-time on an individual basis, as was done in this study, this method is very time-consuming and labor-intensive. Thus, researchers sometimes use shortcuts such as multiplying the number of people under observation by an estimate of the average follow-up time.

In the hypothetical example portrayed in Figure 2–3, five individuals who were followed for varying amounts of time accrued 30 person-years of follow-up. However, depending on the size of the population and length of follow-up, the 30 person-years could have been accrued in many different ways, such as...
five people each contributing 6 years, three people each contributing 10 years, and so forth. Regardless of how the person-time is accrued (e.g., from 5 or 50 people), the person-time units are assumed to be equivalent. This assumption is usually reasonable, except in extreme situations in which a small number of people are followed for a long period of time.

The particular time unit used to measure person-time can vary, but decisions are guided by how long it takes for the disease to develop. For example, person-years are commonly used for diseases that take many years to develop (such as cancer), and person-months or person-days are used for diseases that develop rapidly (such as infection).

The number of person-time units in the denominator is arbitrary. For example, the same incidence rate can be expressed in terms of 1 person-year, 10 person-years, or 100 person-years. Epidemiologists generally use 100,000 person-years for rare diseases and those that take a long time to develop.

**Relationship Between Cumulative Incidence and Incidence Rate**

It is possible to obtain cumulative incidence from an incidence rate. The simplest situation to demonstrate this relationship is in a fixed population with a constant incidence rate and small cumulative incidence (less than 10%). Here, the mathematical relationship is as follows:

\[ CI = IR_i \times t_i \]

where \( CI \) is cumulative incidence, \( IR_i \) is incidence rate, and \( t_i \) is the specified period of time.

When the incidence rate is not constant, it is necessary to take into account the different rates that prevail during each time period:

\[ CI = \sum (IR_i \times t_i) \]

For example, the mortality rate (a type of incidence rate) among Hiroshima residents was much higher shortly after the atomic bomb explosion than during subsequent years (see Figure 2–2).

**Incidence Summary**

In summary, two measures of disease frequency—cumulative incidence and incidence rate—focus on measuring the transition from health to disease. These measures have complementary strengths and weaknesses. The cumulative incidence is easy to calculate and understand, although it is less accurate when its assumptions are not met. Although the incidence rate has greater accuracy, its person-time denominator is more difficult to calculate and understand. Finally, the incidence rate is most useful for dynamic populations, and cumulative incidence is usually reserved for fixed populations.
Prevalence

While incidence measures the frequency with which new disease develops, prevalence measures the frequency of existing disease. It is simply defined as the proportion of the total population that is diseased. There are two types of prevalence measures—point prevalence and period prevalence—that relate prevalence to different amounts of time (see Figure 2–4). Point prevalence refers to the proportion of the population that is diseased at a single point in time and can be thought of as a single snapshot of the population. The point can be either a particular calendar date such as July 1, 2011, or a point in someone’s life such as college graduation. Period prevalence refers to the proportion of the population that is diseased during a specified duration of time, such as during the year 2011. The period prevalence includes the number of cases that were present at any time over the course of the year.

Mathematically, point prevalence is expressed as follows:

\[
\text{Point prevalence} = \frac{\text{Number of existing cases of disease}}{\text{Number in total population}} \text{ At a point in time}
\]

Period prevalence can be expressed as follows:

\[
\text{Period prevalence} = \frac{\text{Number of existing cases of disease}}{\text{Number in total population}} \text{ During a period of time}
\]

Let’s use these formulas to calculate the point and period prevalence of pneumonia in a nursing home population. The point and period of interest are July 1, 2011 and January 1 through December 31, 2011, respectively. On July 1, 2011, there were 5 cases of pneumonia among the 500 nursing home residents. Thus, the point prevalence of pneumonia was 5/500 or 1% on that date. During the period January 1 through December 31, 2011, there...
were 45 cases of pneumonia among the 500 nursing home residents, and so the period prevalence was 45/500 or 9% during the year. Note that, in this example, the size of the nursing home population remained stable over the year but if it gained or lost members the average size of the nursing home population during 2011 would be the appropriate denominator for the period prevalence measure.

Note that the numerator (existing cases) is a subset of the denominator (total population). Unlike the numerator for the two incidence measures, the prevalence numerator includes all currently living cases regardless of when they first developed. The denominator includes everyone in the population—sick, healthy, at risk, and not at risk. Because prevalence is a proportion, it is dimensionless, and its possible values range from 0 to 1, or 0 to 100% (see Table 2-5).

**Relationship Between Prevalence and Incidence**

Prevalence depends on the rate at which new cases of disease develop (the incidence rate) as well as the duration or length of time that individuals have the disease. The duration of a disease starts at the time of diagnosis and ends when the person either is cured or dies. Mathematically, the relationship between prevalence and incidence is as follows:

\[
\frac{P}{(1 - P)} = IR \times D
\]

where \(P\) is prevalence (the proportion of the total population with the disease), \((1 - P)\) is the proportion of the total population without the disease, \(IR\) is incidence rate, and \(D\) is the average duration (or length of time) that an individual has the disease.

This equation assumes that the population is in steady state (i.e., inflow equals outflow) and that the incidence rate and duration do not change over time. If the frequency of disease is rare (i.e., less than 10%), the equation simplifies to

\[
P = IR \times D
\]

To better understand this relationship, think of the variables that influence the level of water in a sink (see Figure 2-5). The water level is influenced by both the inflow from the faucet and the outflow down the drain. The water level will be high if the inflow is large, if the outflow is low, or if both occur. The water level will be low if inflow is low, outflow is high, or both. Now consider the water level in the sink as prevalence, the incoming water as incidence, and the outflowing water as diseased people who either are cured or die. The number of cases of people currently living with a disease (prevalence) will be influenced by the rate at which new cases develop as well as by the rate at which they are eliminated through cure or death.
Consider the real-life example of AIDS, whose prevalence has increased steadily over time (see Figure 2–6). In the early 1990s, the prevalence of AIDS increased because the AIDS case definition was expanded and because incidence increased. Thus, prevalence increased
because *inflow increased*. Since the mid-1990s, prevalence increased because improvements in treatment resulted in dramatic reductions in the number of AIDS deaths. Thus, since the mid-1990s, prevalence increased because *outflow decreased*. In fact, prevalence increased despite stable incidence during this period.

**Uses of Incidence and Prevalence**

Epidemiologists and other public health professionals use each measure of disease frequency for specific purposes (see Table 2–5). Incidence is most useful for evaluating the effectiveness of programs that try to prevent disease from occurring in the first place. In addition, researchers who study the causes of disease prefer to study new cases (incidence) over existing ones (prevalence) because they are usually interested in exposures that lead to developing the disease. Prevalence obscures causal relationships because it combines incidence and survival. In addition, many researchers prefer to use incidence because the timing of exposures in relation to disease occurrence can be determined more accurately.

On the other hand, prevalence is useful for estimating the needs of medical facilities and for allocating resources for treating people who already have a disease. In addition, researchers who study diseases such as birth defects (wherein it is difficult to gather information on defects present in miscarried and aborted fetuses) and chronic conditions such as arthritis (whose beginnings are difficult to pinpoint) have no choice but to use prevalence. Unfortunately, results of such studies are difficult to interpret because it is unclear how much the association is influenced by using a group of survivors.

**Commonly Used Measures of Disease Frequency in Public Health**

There are many measures of disease frequency that are commonly used in the public health disciplines. Some are incidence measures, some are prevalence measures, some are ratios. Descriptions and examples of the major measures follow. Note that the word *rate* is often used incorrectly to describe a proportion or ratio.

**Crude mortality (or death) rate:** Total number of deaths from all causes per 100,000 population per year. The term *crude* means that the rate is based on raw data. In 2007, a total of 2,423,712 deaths occurred among people residing in the United States, resulting in a crude mortality rate of 803.6/100,000 population/year.\(^\text{19}\)

**Cause-specific mortality (or death) rate:** Number of deaths from a specific cause per 100,000 population per year. In 2007, there were 616,067 deaths
from heart disease among U.S. residents, resulting in a cause-specific mortality rate of 204.3/100,000/year.\textsuperscript{19}

\textit{Age-specific mortality (or death) rate}: Total number of deaths from all causes among individuals in a specific age category per 100,000 population per year in the age category. In 2007, there were 29,153 deaths among U.S. children under the age of 1 year, resulting in an age-specific death rate of 680.0/100,000/year.\textsuperscript{19}

\textit{Years of potential life lost}: The number of years that an individual was expected to live beyond his or her death. In 2007, a total of 1,113 years were lost due to heart disease, 1,574 years were lost due to cancer, and 1,156 were lost due to unintentional injuries before age 75 per 100,000 population younger than 75 years of age.\textsuperscript{19} The number of years of potential life lost reflects both the number of individuals who died of a particular cause and the age at which the death occurred. For example, a cause of death that is more common among children and young adults (such as unintentional injuries) will result in more years of life lost per individual than a cause of death that is common among the elderly (such as heart disease).

\textit{Livebirth rate}: Total number of livebirths per 1,000 population per year. A livebirth is a pregnancy that results in a child who, after separation, breathes or shows any other evidence of life. Sometimes the denominator includes only women of childbearing age. In 2007, a total of 4,316,233 livebirths occurred among women who are residents of the United States, and the crude livebirth rate was 14.3/1,000/year.\textsuperscript{19}

\textit{Infant mortality rate}: Number of deaths of infants less than 1 year of age per 1,000 livebirths per year. This statistic is often divided into neonatal deaths (those occurring during the first 27 days following birth) and post-neonatal deaths (those occurring from 28 days through 12 months). In 2006, the infant mortality rate in the United States was 6.7/1,000 livebirths/year, the neonatal mortality rate was 4.5/1,000 livebirths/year, and the postneonatal death rate was 2.2/1,000 livebirths/year.\textsuperscript{17}

\textit{Birth defect (also called congenital anomaly or malformation) rate}: Number of children born with defects per 10,000 births. The numerator and denominator often include both live- and stillbirths. According to a nationwide birth defects monitoring program, the prevalence of spina bifida, a central nervous system malformation, was 3.72/10,000 live births during 2004–2006.\textsuperscript{20}

\textit{Morbidity rate}: Number of existing or new cases of a particular disease or condition per 100 population. The time period that is covered and the population size in the denominator vary. \textit{Morbidity} is a general word that can apply to a disease, condition, or event. For example, from 2005 to 2008, the prevalence of physician-diagnosed diabetes among U.S. adults aged 65 years and over was 26.9\%.\textsuperscript{19}
Attack rate: Number of new cases of disease that develop (usually during a defined and short time period) per the number in a healthy population at risk at the start of the period. This cumulative incidence measure is usually reserved for infectious disease outbreaks. For example, the 24-hour attack rate for food poisoning was 50% among people who ate chicken salad at the banquet.

Case fatality rate: Number of deaths per number of cases of disease. Note that this measure is a type of cumulative incidence, so it is necessary to specify the length of time to which it applies. For example, the 1-year case fatality rates following an acute myocardial infarction (heart attack) were 34.8% in Black men and 28.7% in White men according to a recent U.S. study.²¹

Survival rate: Number of living cases per number of cases of disease. This rate is the complement of the case fatality rate; also a cumulative incidence measure. Five-year relative survival rates for cancer compare people with a particular cancer to similar people in the general population. For example, from 2001 to 2007, 5-year relative survival rates for prostate cancer were 100% among men diagnosed while the tumor was still confined to the prostate or had spread only to the regional lymph nodes, and 28.8% among men whose tumor had metastasized to distant sites.¹⁴

Summary

A population is defined as a group of people with a common characteristic such as place of residence, age, or the occurrence of an event. There are two main types of populations, fixed and dynamic (or open). The membership of a fixed population is defined by a life event and is permanent, whereas the membership of a dynamic population is defined by a changeable characteristic and is transient.

Three factors should always be considered when measuring how commonly a disease occurs in a population: (1) the number of affected individuals or cases, (2) the size of the population from which the cases arise, and (3) the amount of time that this population is followed. Before epidemiologists can count the number of affected cases, they must compose a disease definition that is usually based on physical and pathological examinations, diagnostic tests, and signs and symptoms. Disease definitions often change over time as more is learned about a disease and its manifestations. For example, the official case definition of AIDS expanded when its cause was discovered and improvements in detection were made.

Incidence and prevalence are the two basic measures of disease frequency. Incidence measures the occurrence of new disease and so captures the transition from health to disease. Cumulative incidence and incidence rate are the two main types of incidence measures. Cumulative
incidence is defined as the proportion of a candidate population that becomes diseased over a specified time period. It is a dimensionless proportion that measures the average risk of contracting a disease over a certain time period. Incidence rate is the occurrence of new cases of disease that arise during person-time of observation, and so it is a true rate. It is important to remember that person-time accumulates only among candidates for disease. Cumulative incidence and incidence rate are related mathematically. Both measures are most useful for evaluating the effectiveness of disease-prevention activities and for etiological studies of disease.

Prevalence measures existing disease and so focuses on the period when a person is ill. Prevalence measures the proportion of the total population that is diseased at a point in time or during a period of time. Its numerator consists of the number of existing cases, and its denominator includes the total population, including sick, healthy, at-risk, and immune individuals. Point prevalence refers to a single point in time and is like a snapshot. Period prevalence refers to a specific duration of time that may be derived from a series of snapshots. Prevalence is typically used for estimating the needs of medical facilities and for allocating resources for treating diseased individuals. The incidence rate and prevalence are mathematically related.

Many measures of disease frequency are commonly used in public health, including the crude, cause-specific, and age-specific mortality rates; morbidity rate; livebirth rate; infant mortality rate; attack rate; case fatality rate; and survival rate. Note that the term rate is often incorrectly used to refer to proportions and ratios.

References

Chapter Questions

1. What measure of disease frequency is each of the following?
   A. The percentage of freshman girls who become pregnant over the course of their high school years
   B. The percentage of senior boys who are fathers at the time of graduation
   C. The number of liveborn babies who die of sudden infant death syndrome during the first year of life per 100,000 baby-years of follow-up
   D. The percentage of infants weighing less than 2,500 grams at birth
   E. The lifetime risk of breast cancer
2. Briefly describe the main similarities and differences between each of the following:
   A. Prevalence and incidence
   B. Incidence rate and cumulative incidence
   C. Fixed and dynamic population

3. In 2010, there were 2,900 new cases of breast cancer diagnosed among women in Alabama and 200 new cases diagnosed among women in Alaska. Based on these data, is it accurate to say that the incidence rate of breast cancer is higher in Alabama than Alaska? Why or why not?

4. Consider a class with 100 enrolled students. None of the students were ill at the beginning of the school year. On September 30, a total of five students reported having gastroenteritis. All continued to be ill on October 1, but all five recovered within 3 days. On October 14, another three students developed gastroenteritis. All of these students continued to be ill on October 15, but all three recovered 5 days later. In this example, assume that a person cannot get gastroenteritis more than once.
   A. Calculate the prevalence of gastroenteritis in the class on October 1.
   B. Calculate the prevalence of gastroenteritis in the class on October 30.
   C. Calculate the cumulative incidence of gastroenteritis in the class during the month of October.

5. The incidence rate of a nonfatal disease is 500/100,000 person-years. People usually have the disease for an average of 3 years, at which time the disease resolves spontaneously. Estimate the prevalence of this disease using this information. Assume that the population is in steady state.

6. A population of 100 healthy men was followed for the development of prostate cancer. After being followed for 5 years, 20 men developed prostate cancer. Another 10 men were followed for 1 year and then were lost. The remaining men who never developed the disease were followed for 10 years. Calculate the number of person-years of observation accrued by this population.

7. Consider the following hypothetical data on the occurrence of hepatitis in two cities:

<table>
<thead>
<tr>
<th>City</th>
<th>New cases</th>
<th>Observation period</th>
<th>Starting population at risk</th>
</tr>
</thead>
<tbody>
<tr>
<td>City A</td>
<td>25</td>
<td>January–December 2010</td>
<td>25,000</td>
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<tr>
<td>City B</td>
<td>30</td>
<td>January–December 2010</td>
<td>50,000</td>
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</tbody>
</table>
A. Calculate the cumulative incidence of hepatitis in each city.
B. Which city has the higher cumulative incidence?

8. A total of 60 cases of myocardial infarction were reported over a period of 2 years in a city with a population of 100,000 people. Using these data, estimate the incidence rate of myocardial infarction per 100,000 person-years. State any assumptions that are needed.

9. The incidence rate of post-partum depression among 250,000 women who recently experienced a pregnancy was 12 cases per 100,000 woman-years of follow-up. Exactly how many incident cases of post-partum depression developed in this population?

10. State the type of population (fixed or dynamic) that best describes each of the following:
   A. People who live in New York City
   B. Men who had coronary bypass surgery as of 2011
   C. Children who were vaccinated against polio in 1955
   D. Women who are practicing physicians

11. Indicate whether the following statements are true or false:
   A. Only the population at risk contributes to the denominator of the cumulative incidence.
   B. When calculating the incidence rate of a disease, it is necessary to follow all subjects for the same length of time.
   C. If the incidence rate of a very serious disease is 75/100,000 person-years and the prevalence of this disease in the population is 25/100,000, then the average duration of this disease must be 3 years.
   D. All other things being equal, when a new prevention measure for a disease is developed, the prevalence of the disease will decrease over time.
   E. All other things being equal, when a treatment is developed that prolongs the life of people suffering from a disease, the prevalence of the disease will increase over time.

12. An epidemiologic investigation that was started on January 1, 2011, identified a population of 1,000 individuals among whom 4 were found to have the disease under study. During the year of the study, six new cases were found. Among the total of 10 cases, there were 6 deaths during the year. For the 10 cases, the diagram indicates the time of case recognition, periods of observation during the study, and vital status at the time of the termination of observation. An arrow at the start of the
diagram (subjects 1, 2, 3, 4) indicates that the start of disease occurred before the study began.

Assume that the 990 remaining individuals in the study did not become ill or die during the year of observation. From the information and diagram given, calculate the following:

A. Prevalence of the disease on January 1, 2011; July 1, 2011; and December 31, 2011

B. Cumulative incidence of disease during 2011

C. Cumulative incidence of death during 2011

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CHAPTER 2: MEASURES OF DISEASE FREQUENCY